

Advection issues and recent developments in eddy-flux measurements

The background features a stylized illustration of a forest with green trees and brown trunks. A tall, silver measurement tower stands in the center. A black curved arrow points from the left side of the tower towards the right, indicating advection. A white crescent moon is visible in the upper left sky. The ground is depicted in shades of brown and orange, with some green grass patches.

Chuixiang Yi

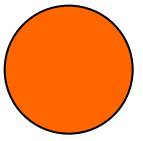
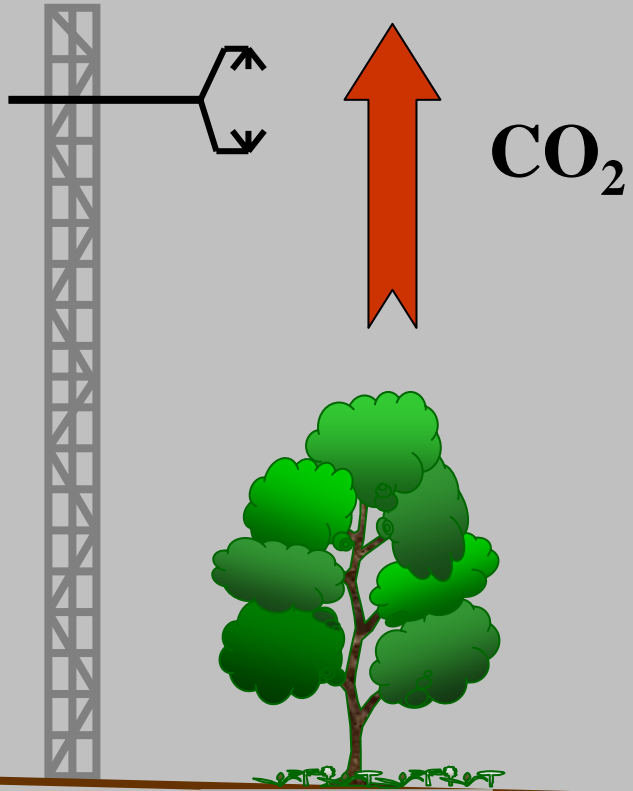
**School of Earth and Environmental Sciences
Queens College, City University of New York**

Courtesy to Jielun Sun



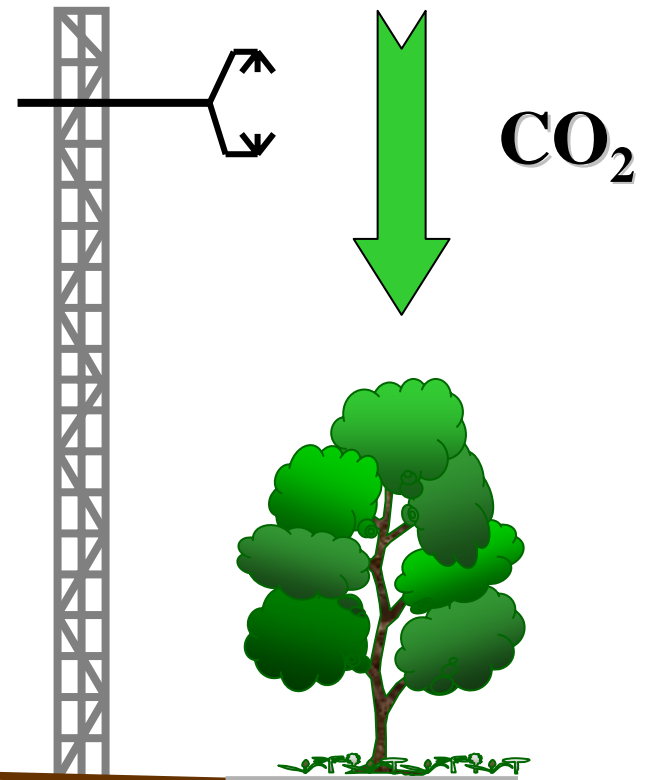
Small u_*

$NEE = \text{Respiration} > 0$



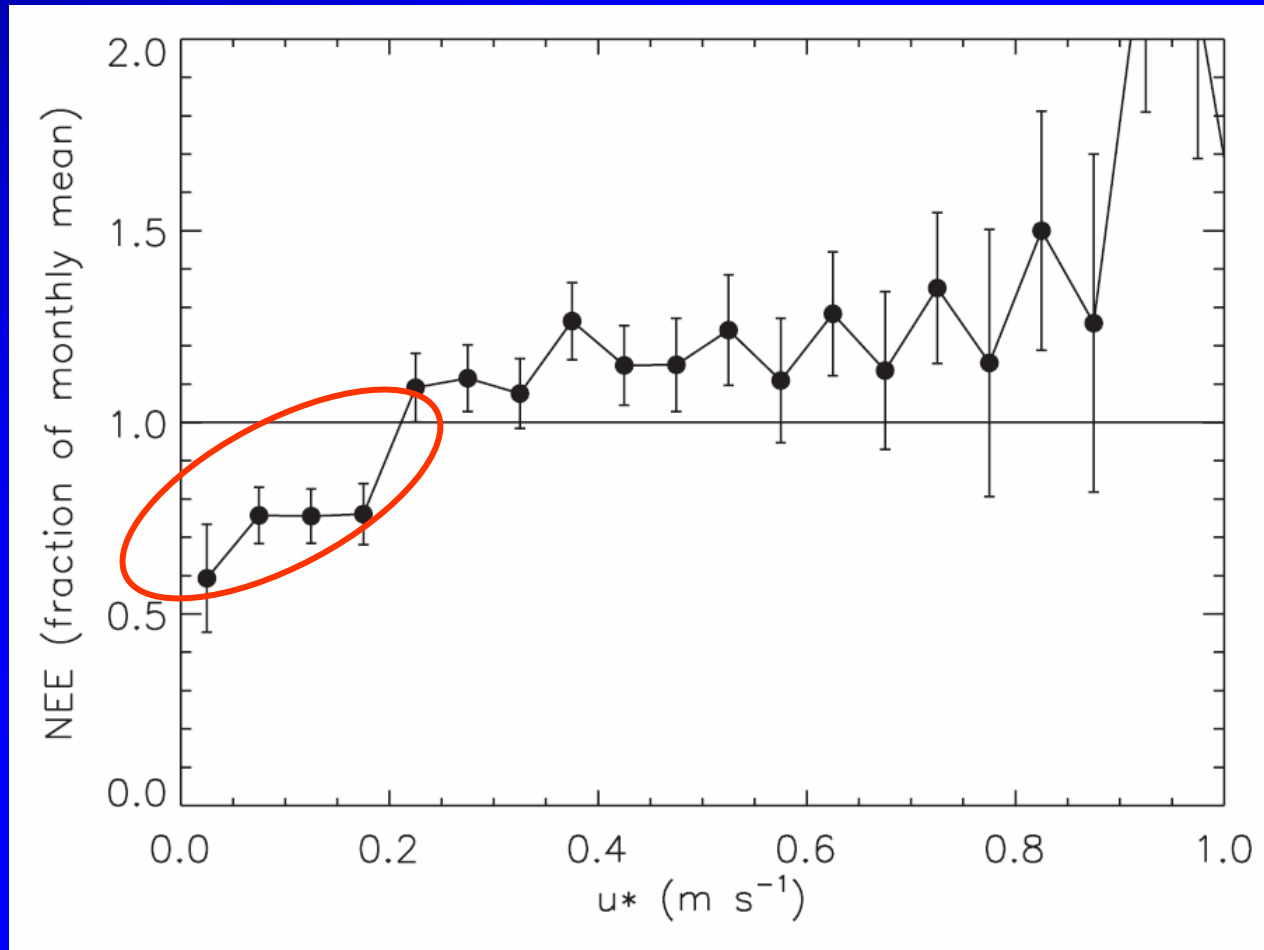
Large u_*

$NEE = \text{Photosynthesis} + \text{Respiration} < 0$

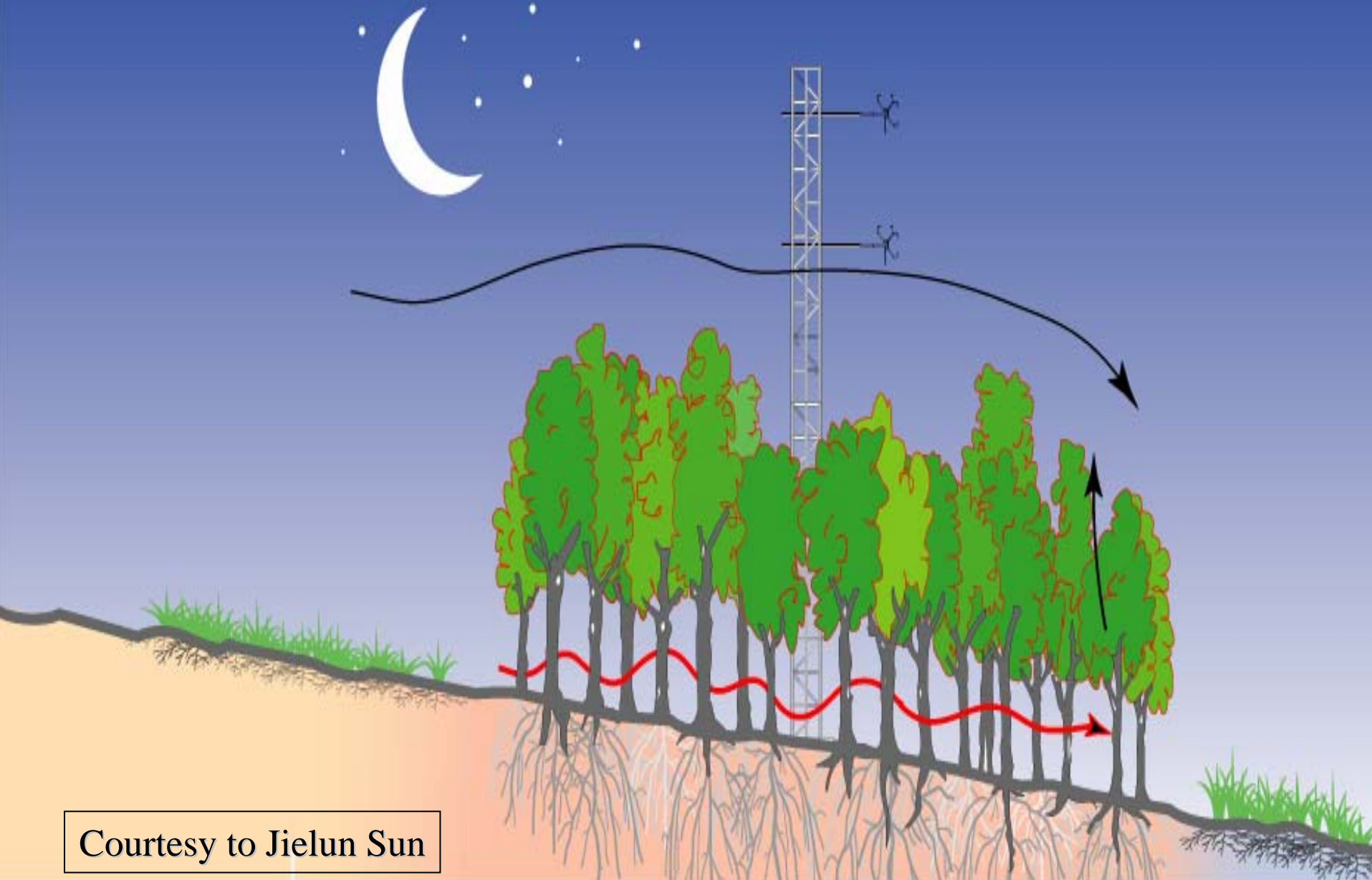


U_* represents the strength of turbulence

Problems: Nighttime Nee is negative in calm conditions



Advection issues on eddy flux measurements



Courtesy to Jielun Sun

Mass conservation law

$$\left[\frac{\partial \bar{c}}{\partial t} + \bar{u} \frac{\partial \bar{c}}{\partial x} + \bar{w} \frac{\partial \bar{c}}{\partial z} + \overline{\frac{\partial w'c'}{\partial x}} + \overline{\frac{\partial w'c'}{\partial z}} \right] = \bar{S}_c$$

Integrate above equation from 0 to Z_r

$$\int_0^{z_r} \left[\frac{\partial \bar{c}}{\partial t} + \bar{u} \frac{\partial \bar{c}}{\partial x} + \bar{w} \frac{\partial \bar{c}}{\partial z} \right] dz + \int_0^{z_r} \overline{\frac{\partial w'c'}{\partial z}} dz = \int_0^{z_r} \bar{S}_c dz$$

$$\int_0^{z_r} \left[\frac{\partial \bar{c}}{\partial t} + \bar{u} \frac{\partial \bar{c}}{\partial x} + \bar{w} \frac{\partial \bar{c}}{\partial z} \right] dz + \overline{w'c'} \Big|_{z_r} - \overline{w'c'} \Big|_0 = \int_0^{z_r} \bar{S}_c dz$$

**NEE
definition**

$$NEE \equiv \int_0^{z_r} \bar{S}_c dz + (\overline{w'c'})_{z=0}$$

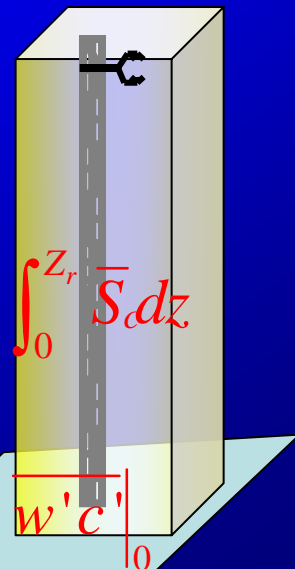
$$= \int_0^{z_r} \frac{\partial \bar{c}}{\partial t} dz + (\overline{w'c'})_{z_r} + \int_0^{z_r} \bar{u} \frac{\partial \bar{c}}{\partial x} dz + \int_0^{z_r} \bar{w} \frac{\partial \bar{c}}{\partial z} dz$$

I

II

III

IV



$$NEE = \int_0^{z_r} \frac{\partial \bar{c}}{\partial t} dz + \overline{(w'c')}_{z_r} + \int_0^{z_r} \left\{ \bar{u} \frac{\partial \bar{c}}{\partial x} + \bar{w} \frac{\partial \bar{c}}{\partial z} \right\} dz$$



Eddy flux



Measured

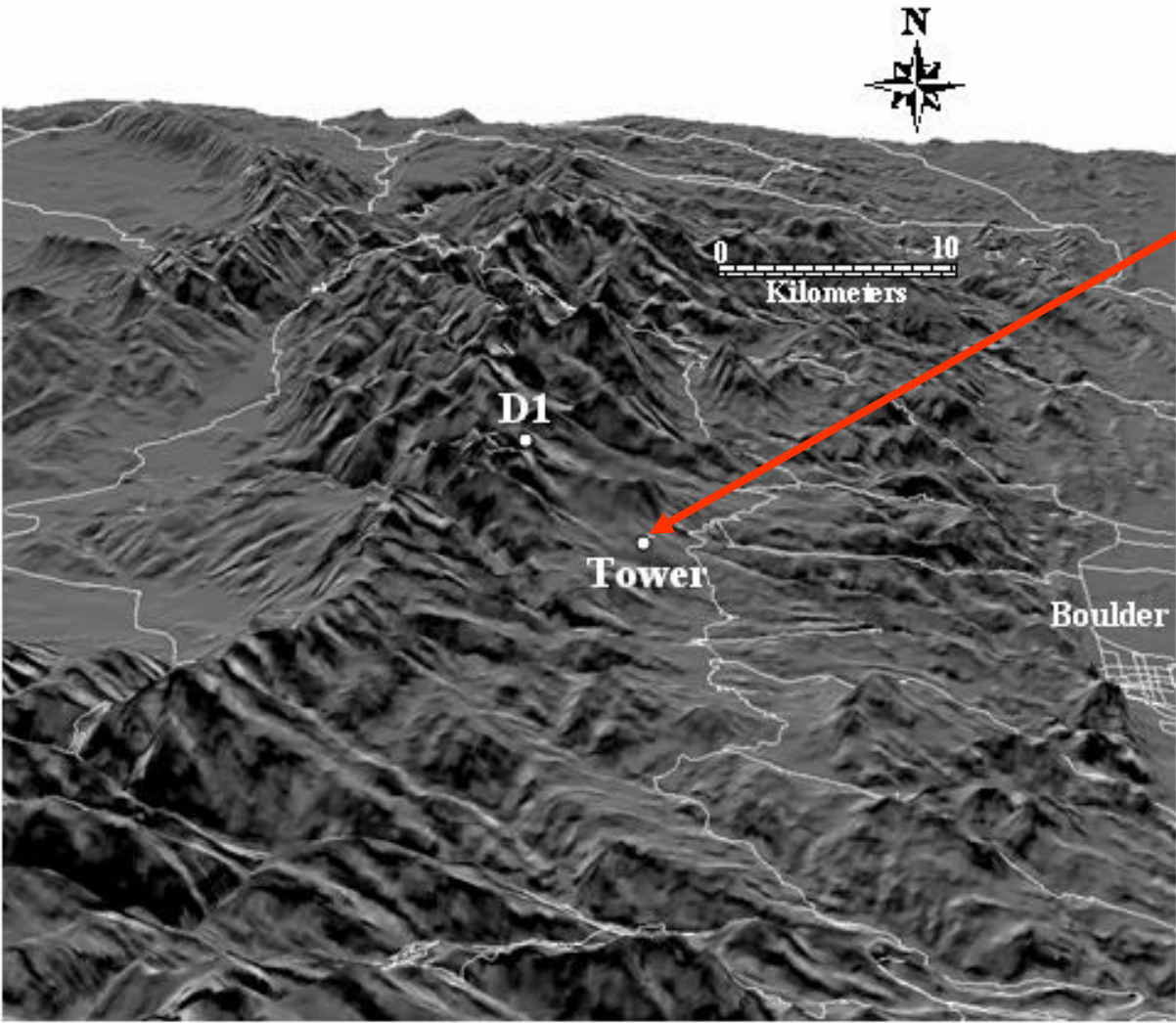


Advection terms



Neglected

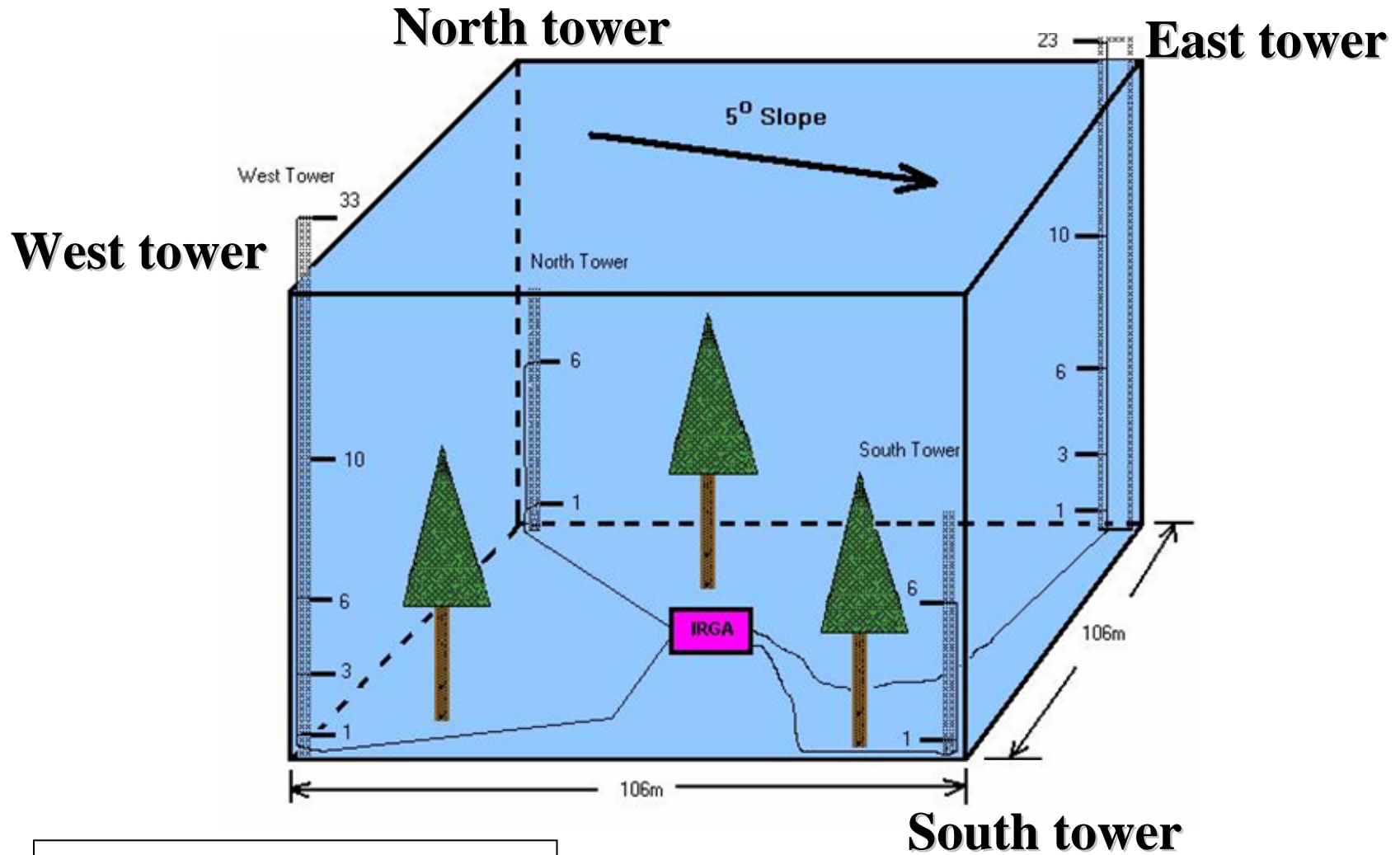
Examining advection issues at Ameriflux Niwot Ridge site



An aerial photograph of a vast, dense coniferous forest. Two tall, slender towers are visible, one on the left and one on the right, rising above the tree canopy. In the background, a range of mountains with a mix of green and brown slopes stretches across the horizon under a clear blue sky. The text 'Niwot Ridge AmeriFlux Site' is overlaid in a black, italicized serif font across the middle of the image.

Niwot Ridge AmeriFlux Site

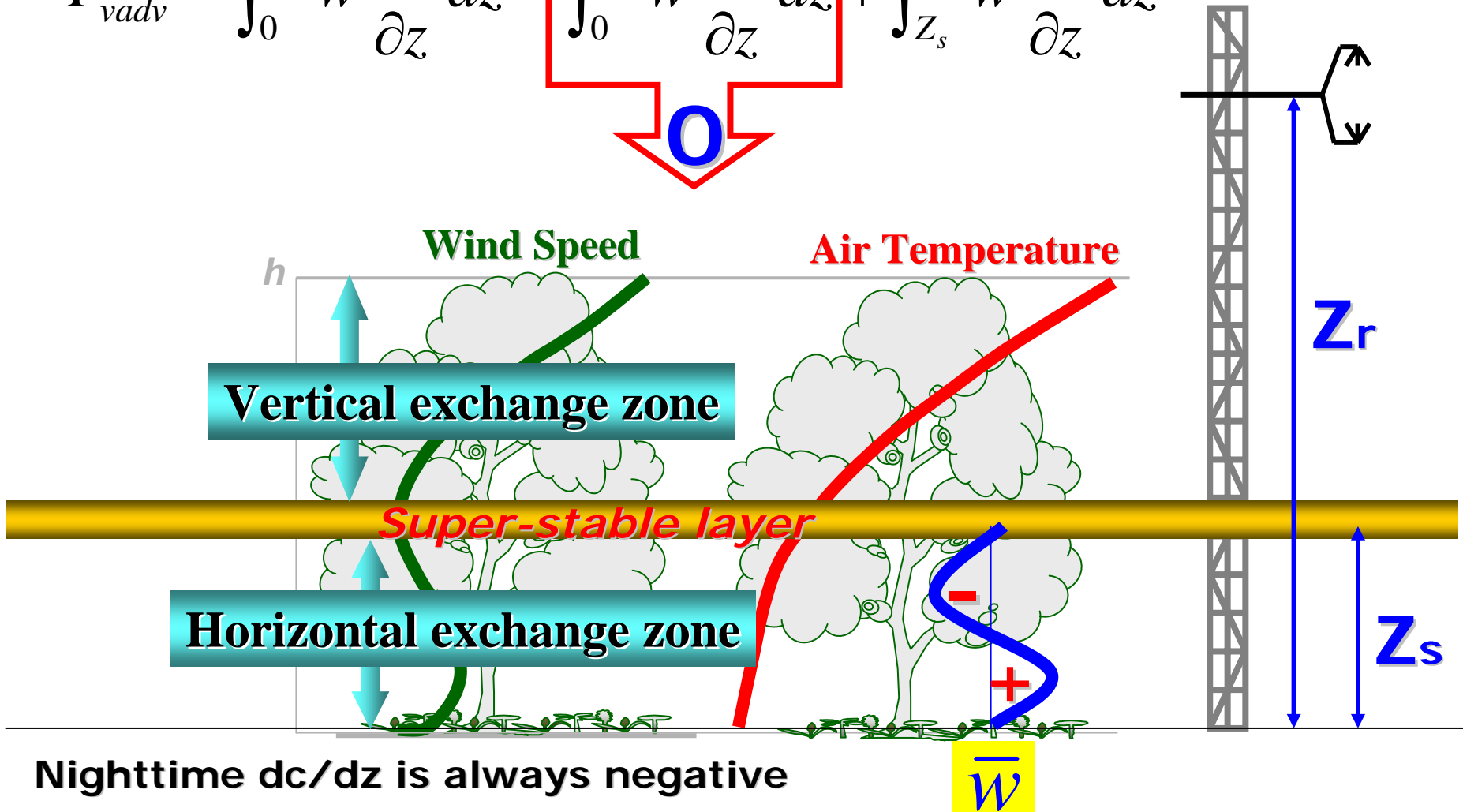
3-D measurement system



Courtesy to Dean Anderson

Vertical advection

$$F_{vadv} = \int_0^{z_r} \bar{w} \frac{\partial \bar{c}}{\partial z} dz = \int_0^{z_s} \bar{w} \frac{\partial \bar{c}}{\partial z} dz + \int_{z_s}^{z_r} \bar{w} \frac{\partial \bar{c}}{\partial z} dz$$



Vertical advection

$$F_{vadv} = \int_{Z_s}^{Z_r} \bar{w} \frac{\partial \bar{c}}{\partial z} dz = \int_{Z_s}^{Z_r} \frac{\partial \bar{w} \bar{c}}{\partial z} dz - \int_{Z_s}^{Z_r} \bar{c} \frac{\partial \bar{w}}{\partial z} dz$$

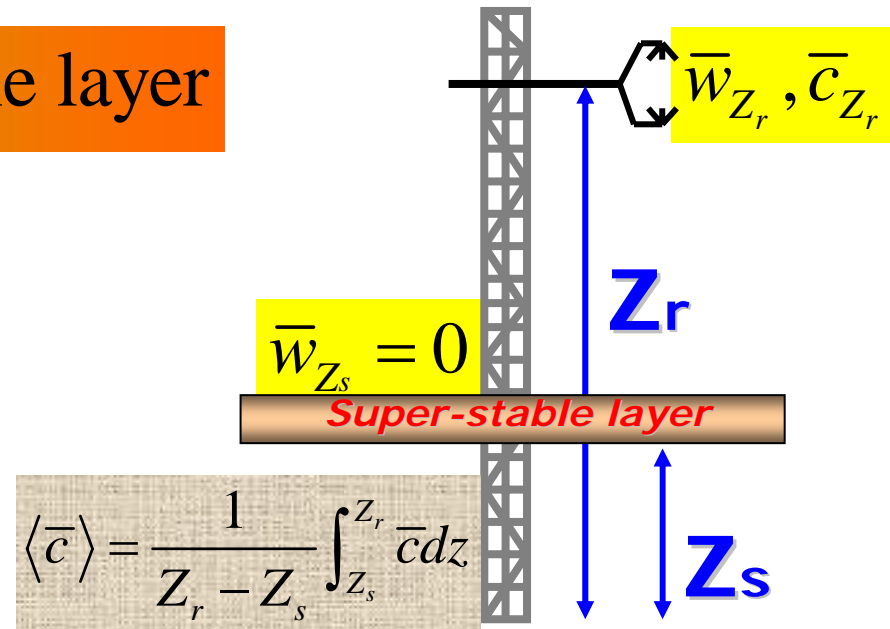
$$F_{vadv} = \bar{w}_{Z_r} \bar{c}_{Z_r} - \bar{w}_{Z_s} \bar{c}_{Z_s} - \frac{\bar{w}_{Z_r} - \bar{w}_{Z_s}}{Z_r - Z_s} \int_{Z_s}^{Z_r} \bar{c} dz$$

Lee's assumption

$$\frac{\partial \bar{w}}{\partial z} = \frac{\bar{w}_{Z_r} - \bar{w}_{Z_s}}{Z_r - Z_s}$$

$\bar{w}_{Z_s} = 0$ at super-stable layer

$$\begin{aligned} F_{vadv} &= \bar{w}_{Z_r} \bar{c}_{Z_r} - \frac{\bar{w}_{Z_r}}{Z_r - Z_s} \int_{Z_s}^{Z_r} \bar{c} dz \\ &= \bar{w}_{Z_r} \bar{c}_{Z_r} - \bar{w}_{Z_r} \langle \bar{c} \rangle \\ &= \bar{w}_{Z_r} (\bar{c}_{Z_r} - \langle \bar{c} \rangle) \end{aligned}$$



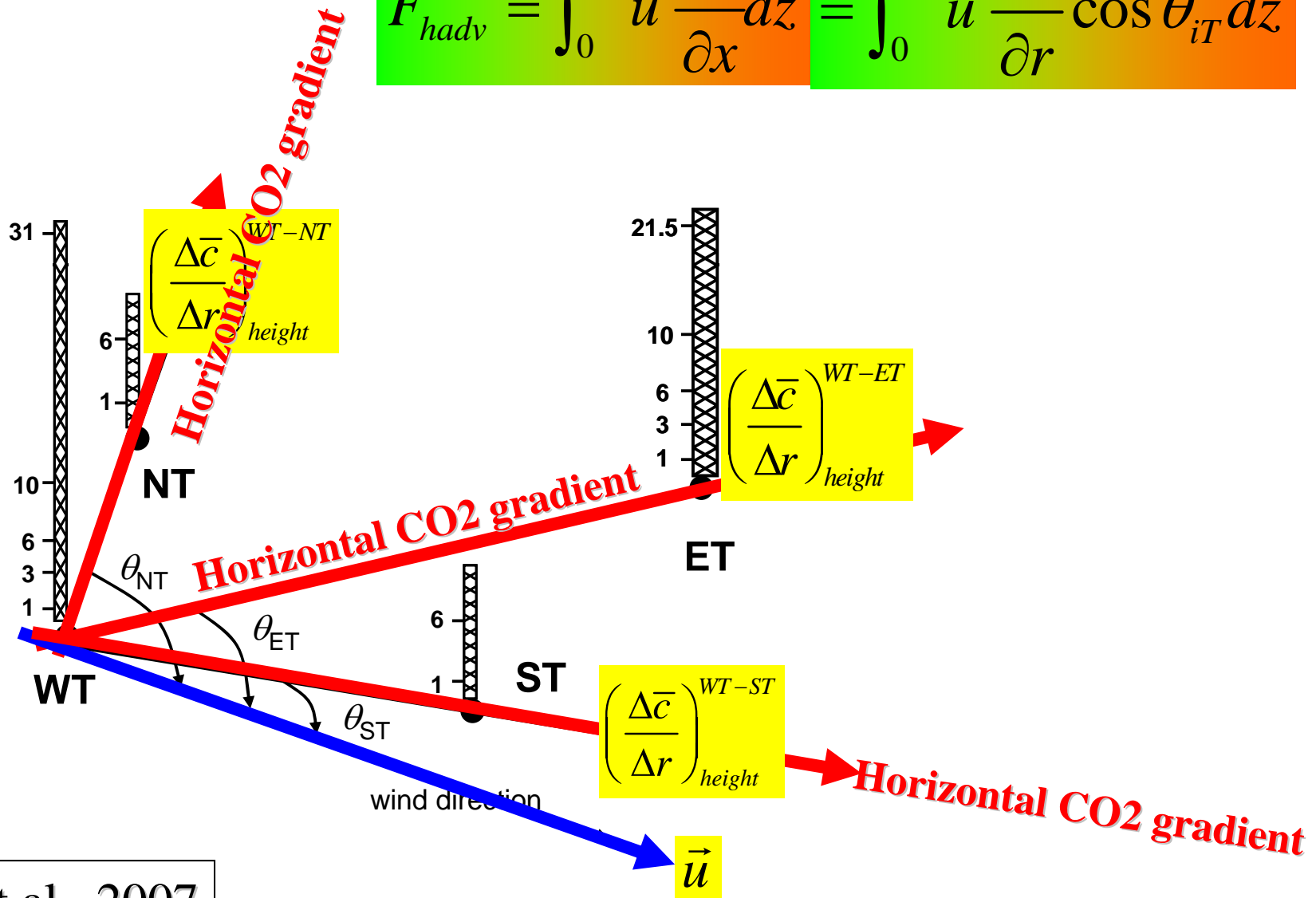
\overline{W} Algorithm

Wilczak, J.M., Oncley, S.P., and Stage, S.A. 2001. Sonic anemometer tilt correction algorithm. *Boundary-Layer Meteorology* 99: 127-150.

Turnipseed, A.A., Anderson, D.E., Burns, S., Blanken, P.D., and Monson, R.K. 2004. Airflows and turbulent flux measurements in mountainous terrain. Part 2. Mesoscale effects. *Agricultural and Forest Meteorology* 125: 187-205.

Horizontal advection calculation

$$F_{hadv} = \int_0^{z_r} \bar{u} \frac{\partial \bar{c}}{\partial x} dz = \int_0^{z_r} \bar{u} \frac{\partial \bar{c}}{\partial r} \cos \theta_{iT} dz$$

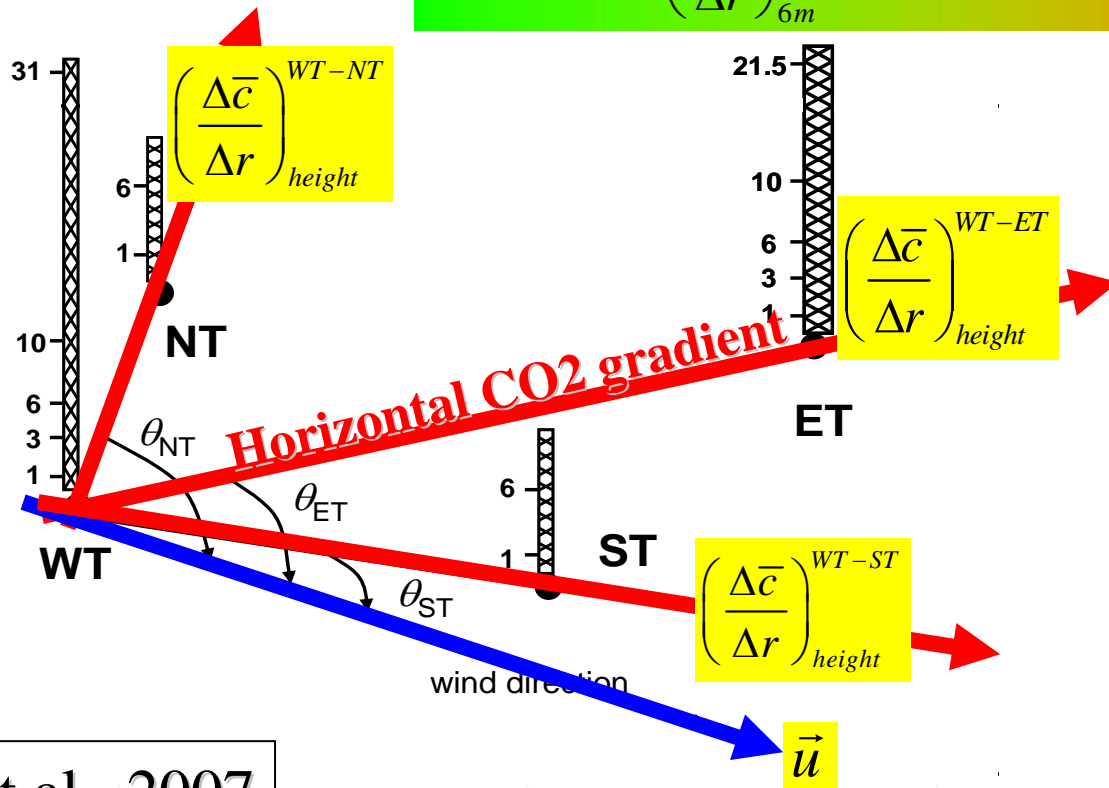


Horizontal advection calculation

$$F_{adv} \approx \int_0^{12} \bar{u} \left. \frac{\partial \bar{c}}{\partial r} \right|_{iT} \cos \theta_{iT} dz$$

$$\approx \bar{u}_{1m} \left(\frac{\Delta c}{\Delta r} \right)_{1m}^{WT-iT} \cos \theta_{iT} * 2 + \bar{u}_{3m} \left(\frac{\Delta c}{\Delta r} \right)_{3m}^{WT-ET} \cos \theta_{ET} * 2$$

$$+ \bar{u}_{6m} \left(\frac{\Delta c}{\Delta r} \right)_{6m}^{WT-iT} \cos \theta_{iT} * 4 + \bar{u}_{10m} \left(\frac{\Delta c}{\Delta r} \right)_{10m}^{WT-ET} \cos \theta_{ET} * 4,$$



The CO2 gradient that is closer to wind direction is first choice to use. For example, the angle can be limited by $|\cos \theta| \geq 0.8$

Another horizontal advection calculation

Projection of CO2 gradient into wind direction

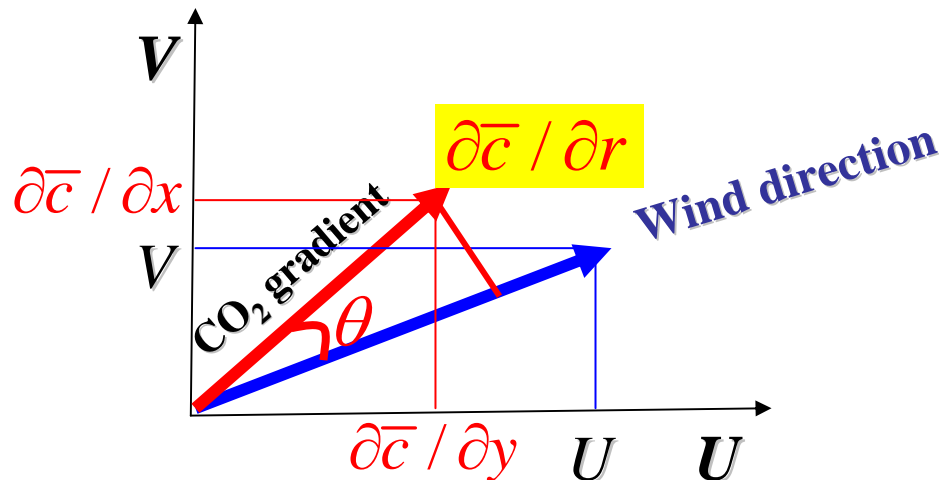
$$\mathbf{U} \cdot \nabla \bar{c} = \bar{u} \left. \frac{\partial \bar{c}}{\partial r} \right|_{iT} \cos(\theta_{iT})$$

dc/dr is CO2 gradient along a pair towers

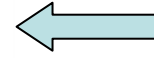
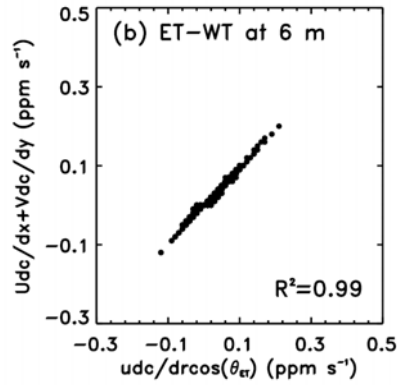
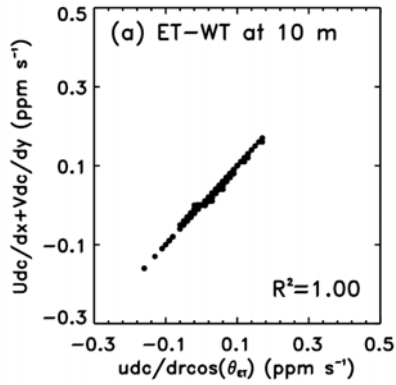
Projection of CO2 gradient into x and y directions

$$\mathbf{U} \cdot \nabla \bar{c} = (U\vec{i} + V\vec{j}) \cdot \left(\frac{\partial \bar{c}}{\partial x} \vec{i} + \frac{\partial \bar{c}}{\partial y} \vec{j} \right) = U \frac{\partial \bar{c}}{\partial x} + V \frac{\partial \bar{c}}{\partial y}$$

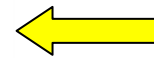
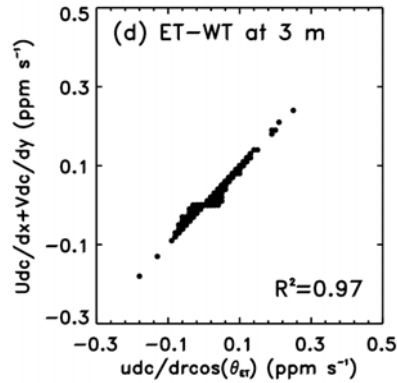
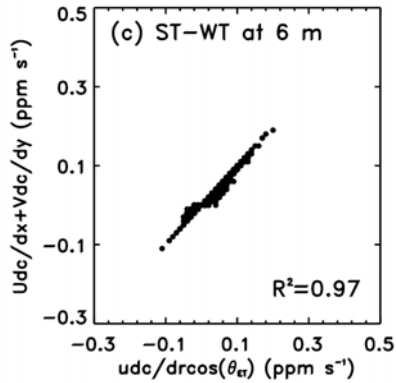
x-y coordinate system is fixed on an instrument



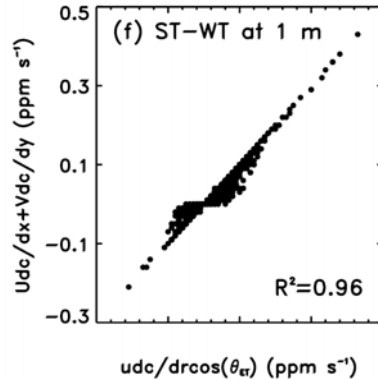
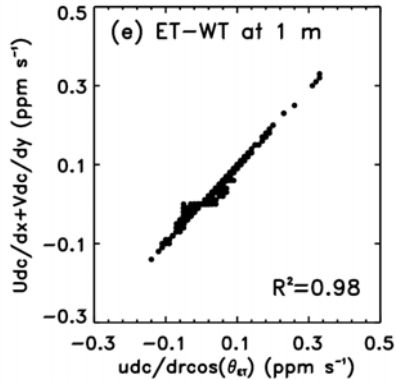
$U_{dc}/dx + V_{dc}/dy$



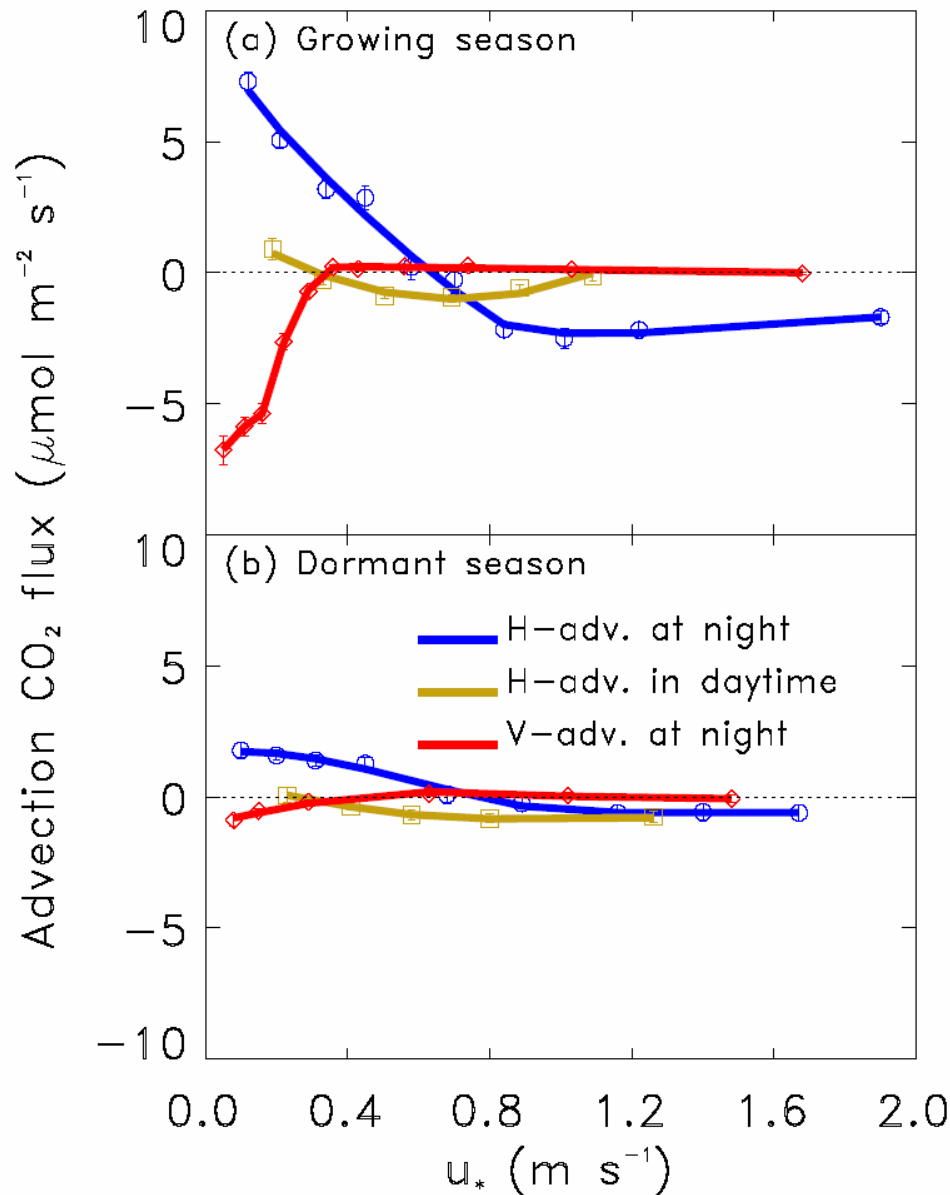
Comparison between two methods



Good agreement between Two algorithms



$u_{dc}/drcos(\theta)$

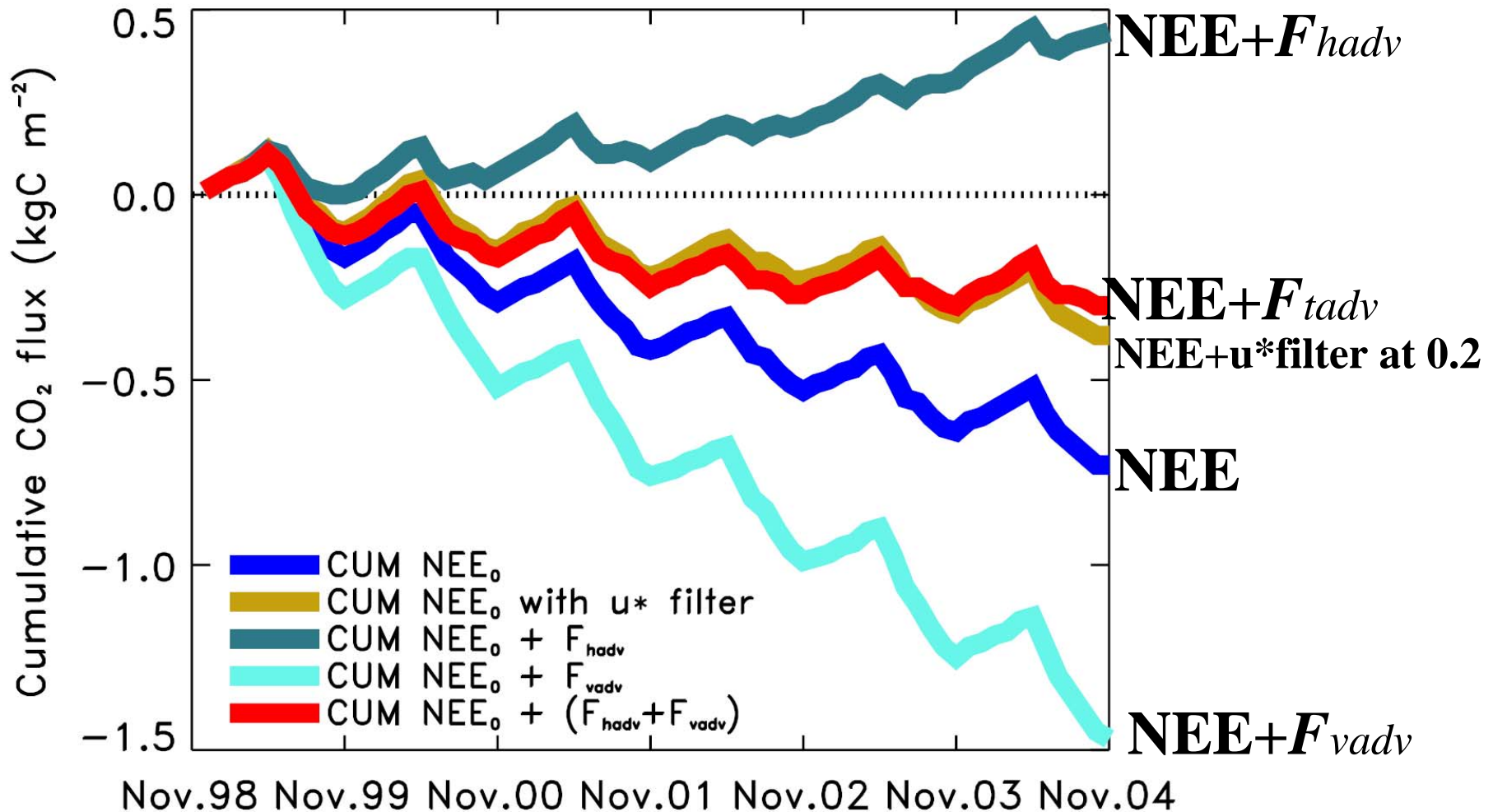


Advection correction is dependent on u^*

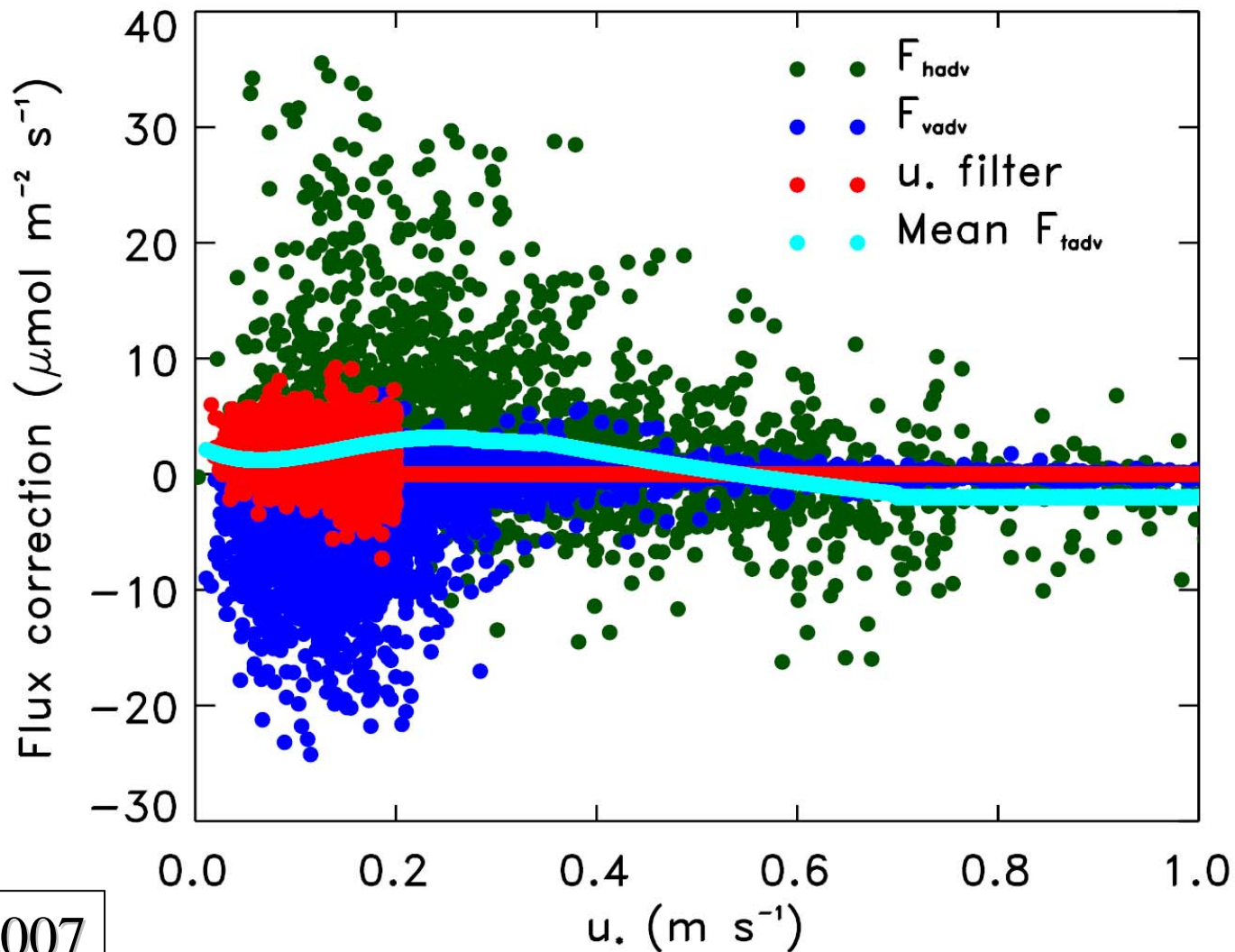
Vertical advection is opposite to horizontal advection

Correction in summer is much larger than in winter

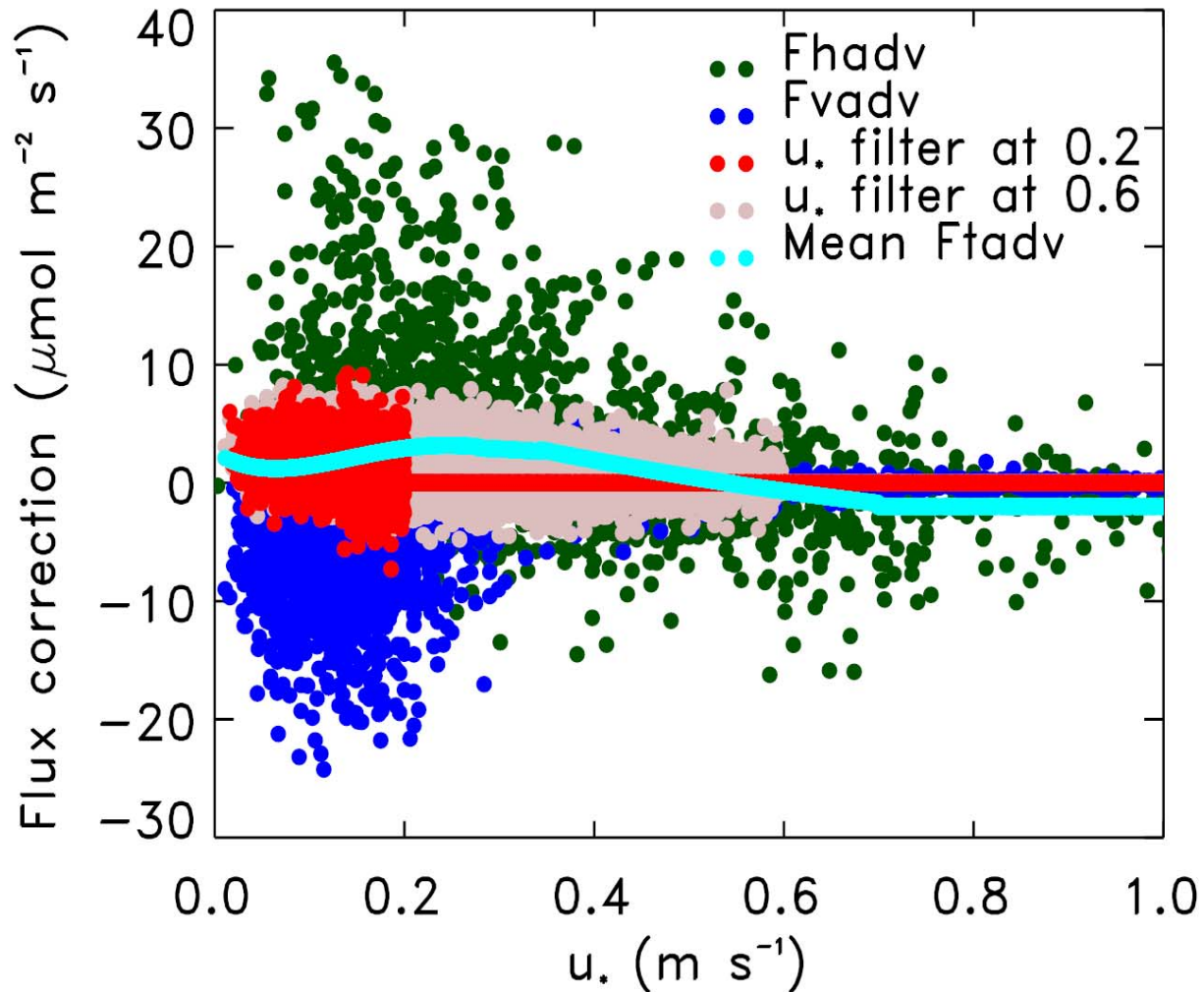
6-year cumulative NEE



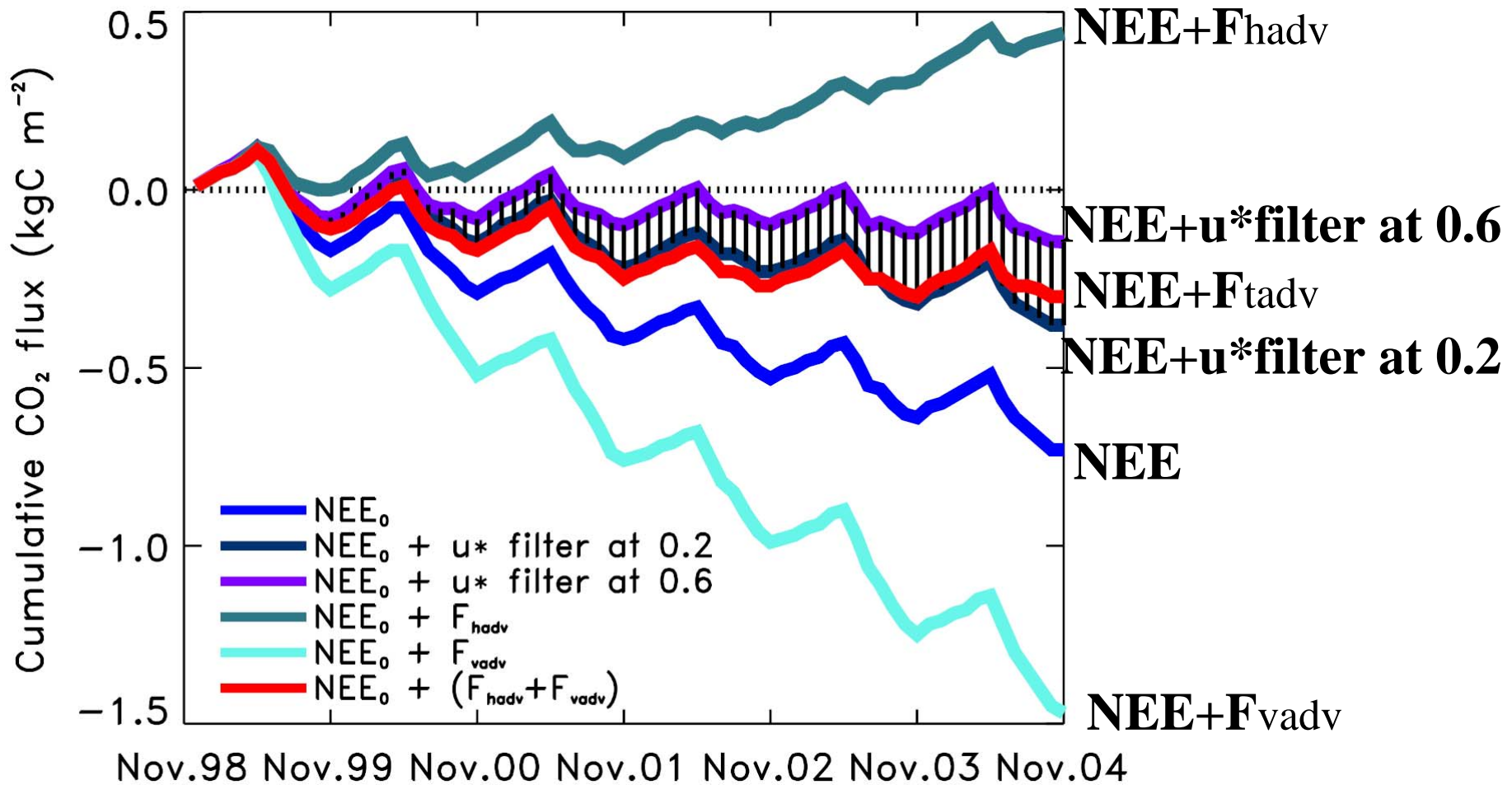
Comparison to u^* filter at 0.2



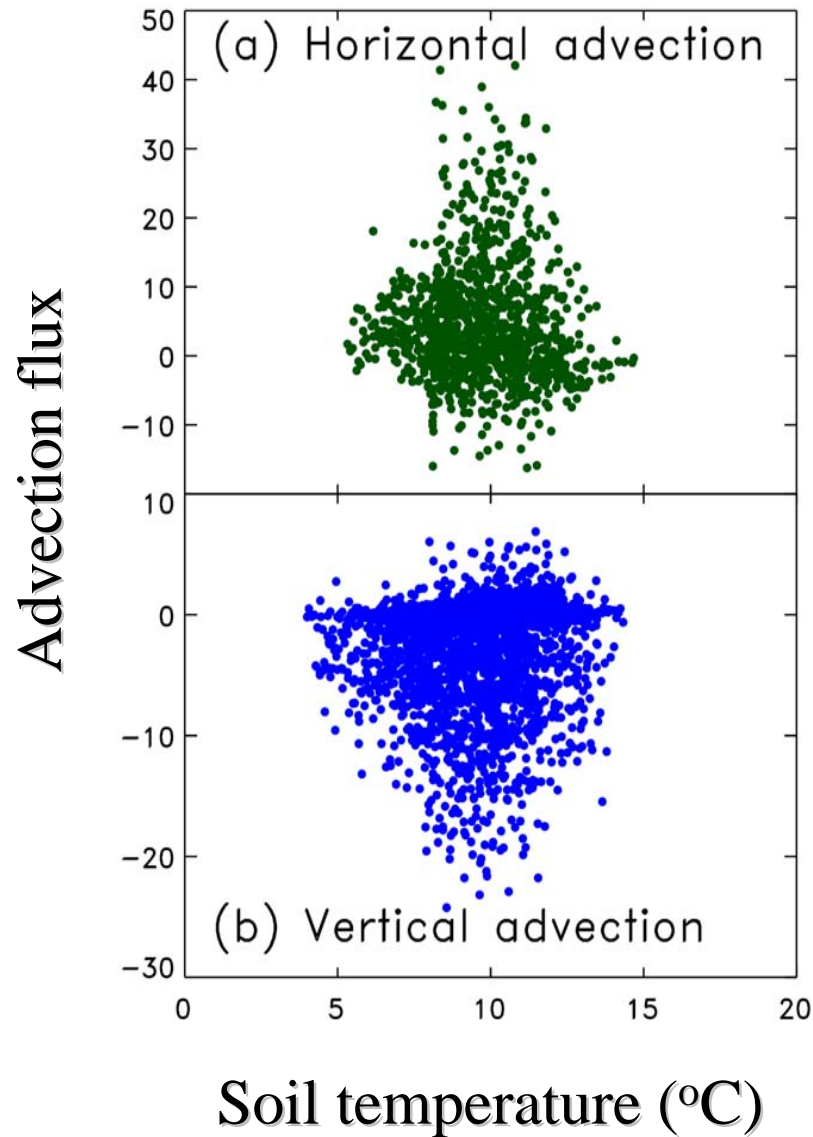
Comparison to u^* filter at 0.6



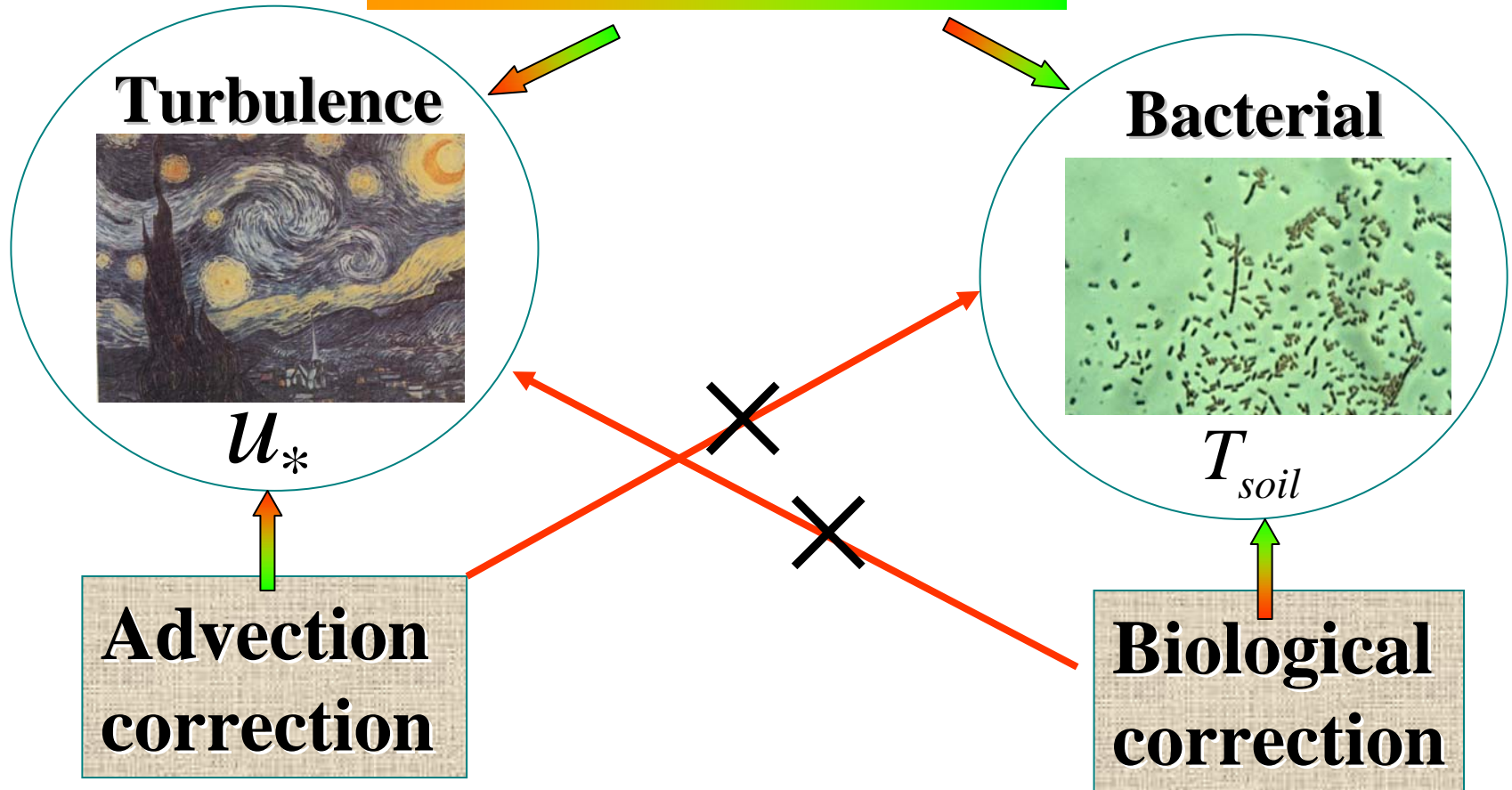
6-year cumulative NEE



Advection flux is not a function of soil temperature



Nocturnal NEE



Flow patterns
Site-specific

Uncertainties
of u_* cutoff

Summary & Conclusions

- **Advection fluxes are functions of u^* , but not functions of temperature.**
- **The sign and magnitude of advection fluxes are related to the convergence/divergence of terrain-induced flows.**
- **Ecological correction is a function of temperature but not a function of u^* .**
- **Ecological correction has no physical base to account for the advection components.**

Contact information

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